## EXPLORING ANGLE PAIRS

## Goal: To learn how to describe different angle pairs, identify geometric relationships, and use these angle pairs to find angle measures.

| Definition | Example |  |
| :---: | :---: | :---: |
| Adjacent angles are two coplanar angles with a common side, a common vertex, and no common interior points. | $\angle 1$ and $\angle 2, \angle 3$ and $\angle 4$ |  |
| Vertical angles are two angles whose sides are opposite rays. | $\angle 1$ and $\angle 2, \angle 3$ and $\angle 4$ |  |
| Complementary angles are two angles whose measures have a sum of 90 . Each angle is called the complement of the other. | $\angle 1$ and $\angle 2, \angle A$ and $\angle B$ |  |
| Supplementary angles are two angles whose measures have a sum of 180 . Each angle is called the supplement of the other. | $\angle 3$ and $\angle 4, \angle B$ and $\angle C$ |  |

## Use the diagram to determine if the statement is true or false. Explain. <br> Ex (a) $\begin{gathered}\angle B F D \text { and } \angle C F D \\ \text { adjacent angles. }\end{gathered}$ <br> 

Ex (b) $\angle A F B$ and $\angle E F D$ are vertical angles.

Ex (c) $\angle A F E$ and $\angle B F C$ are complementary.


Ex (d) $\angle A F E$ and $\angle C F D$ are vertical angles.

Ex le) $\angle B F C$ and $\angle D F E$ are Supplementary.


Ex (f) $\angle B F D$ and $\angle A F B$ are adjacent angles.

## Concept Summary Finding Information From a Diagram

There are some relationships you can assume to be true from a diagram that has no marks or measures. There are other relationships you cannot assume directly. For example, you can conclude the following from an unmarked diagram.

- Angles are adjacent.
- Angles are adjacent and supplementary.
- Angles are vertical angles.

You cannot conclude the following from an unmarked diagram.

- Angles or segments are congruent.
- An angle is a right angle.
- Angles are complementary.


## Ex ia) What can you conclude from the information in the diagram? <br> 

## Ex ib) What can you conclude from the information in the diagram? Circle all that apply. <br> A. $\bar{T} W \cong \overline{W V}$

B. $\overline{P W} \cong \overline{W Q}$
C. $\angle T W Q$ is a right angle.
D. $\overline{T V}$ bisects $\overline{P Q}$.


Def: A linear pair is a pair of adjacent angles whose non-common sides are opposite rays.

Postulate 1-9 Linear Pair Postulate
If two angles form a linear pair, then they are supplementary.

Ex Ba) $\angle K P L$ and $\angle J P L$ are a linear pair, $m \angle K P L=2 x+24$, and $m \angle J P L=4 x+36$. What are the measures of $\angle K P L$ and $\angle J P L$ ?

Ex Bb) $\angle A D B$ and $\angle B D C$ are a linear pair. $m \angle A D B=3 x+14$ and $m \angle B D C=5 x-2$. What are $m \angle A D B$ and $m \angle B D C$ ?

Def: An angle bisector is a ray that divides an angle into two congruent angles.


Ex 4a) $\overrightarrow{A C}$ bisects $\angle D A B$. If $m \angle D A C=58$, what is $m \angle D A B$ ?

Ex Ab) $\overrightarrow{K M}$ bisects $\angle J K L$. If $m \angle J K L=72$, what is $m \angle J K M$ ?

# Ex5a) If the $m \angle A B C=41$, then what is $m \angle C B D$ ? 



# Ex5b) If $m \angle 1=2 x+11$ and $m \angle 2=6 x-1$, and they are complementary angles, then what is the value of $x$ ? 

## Theorem 2-1 Vertical Angles Theorem

Vertical angles are congruent.


Ex6) What are $m \angle C M L$ and $m \angle J M K$ ?


## LESSON CHECK:

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Do you know HOW?
Name a pair of the following types of angle pairs.

1. vertical angles
2. complementary angles
3. linear pair

4. $\overrightarrow{P B}$ bisects $\angle R P T$ so that $m \angle R P B=x+2$ and $m \angle T P B=2 x-6$. What is $m \angle R P T$ ?

Do you UNDERSTAND? (C) PRACTICES
5. Vocabulary How does the term linear pair describe how the angle pair looks?
(C) 6. Error Analysis Your friend calculated the value of $x$ below. What is her error?



